Revisiting Generic Conversion from Non-Adaptive to Adaptively Secure IBS: Tightness and an Extension

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December 21, 2024

Outline

- IBS Abstract Definition and Security Models
- A Quick Review of Generic Adaptive Constructions of IBS
- Issues in Pan and Wagner's IBS Constructions (PQC 2021)
- Addressing the Identified Issues
- Conclusion

Algorithms:

- Setup(κ) \rightarrow (pp, msk)
- KeyGen(pp, msk, id) \rightarrow sk_{id}
- Sign(pp, m, sk_{id}) $\rightarrow \sigma$
- $\bullet \ \, \mathsf{Ver}(\mathsf{pp}, \mathsf{m}, \sigma, \mathsf{id}) = \begin{cases} 1 & \mathsf{accept} \\ 0 & \mathsf{reject.} \end{cases}$

Correctness:

 $\begin{array}{l} \bullet \ \ \, \forall (\mathsf{pp},\mathsf{msk}) \leftarrow \mathsf{Setup}(\kappa), \, \forall \mathsf{id} \in \mathcal{ID}, \\ \forall \mathsf{sk}_{\mathsf{id}} \leftarrow \mathsf{KeyGen}(\mathsf{pp},\mathsf{msk},\mathsf{id}), \, \mathsf{and} \\ \forall \mathsf{m} \in \mathcal{M}, \, \mathsf{we have} \end{array}$

```
\mathsf{Ver}(\mathsf{pp}, \mathsf{m}, \mathsf{Sign}(\mathsf{pp}, \mathsf{m}, \mathsf{sk}_{\mathsf{id}}), \mathsf{id}) = 1.
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public parameters (pp)





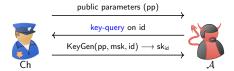
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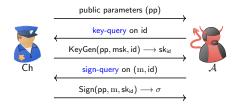
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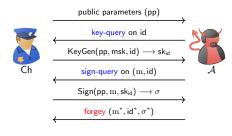


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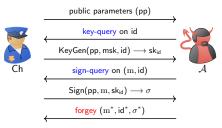
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$$\mathsf{Ver}(\mathsf{pp}, m, \mathsf{Sign}(\mathsf{pp}, m, \mathsf{sk}_{\mathsf{id}}), \mathsf{id}) = 1.$$



$$\mathsf{Adv}^{\mathrm{EUF\text{-}ID\text{-}CMA}}_{\mathcal{A}}(\kappa) := \mathsf{Pr}\left[\mathsf{Ver}(\mathsf{pp}, \mathsf{m}^*, \sigma^*, \mathsf{id}^*) = 1 \wedge \mathsf{id}^* \not\in \mathcal{Q}_{\mathsf{key}} \wedge \left(\mathsf{m}^*, \mathsf{id}^*\right) \not\in \mathcal{Q}_{\mathsf{sign}}\right]$$

• The scheme is EUF-ID-CMA secure, if for all ppt \mathcal{A} , $\mathsf{Adv}^{\mathrm{EUF-ID-CMA}}_{\mathcal{A}}(\kappa)$ is negligible.

EUF-ID-CMA: More Details

Algorithms:

- $\bullet \; \mathsf{Setup}(\kappa) \to (\mathsf{pp}, \mathsf{msk})$
- $\bullet \; \mathsf{KeyGen}(\mathsf{pp},\mathsf{msk},\mathsf{id}) \to \mathsf{sk}_\mathsf{id} \\$
- Sign(pp, m, sk_{id}) $\rightarrow \sigma$
- $\bullet \ \, \mathsf{Ver}(\mathsf{pp}, \mathsf{m}, \sigma, \mathsf{id}) = \begin{cases} 1 & \mathsf{accept} \\ 0 & \mathsf{reject}. \end{cases}$

```
\begin{split} & \frac{\mathsf{Exp}_{\mathcal{A}}^{\mathsf{EUF-ID-CMA}}(\kappa);}{1:\ \mathcal{Q}_{\mathsf{key}} := \emptyset,\ \mathcal{Q}_{\mathsf{sign}} := \emptyset,\ \mathcal{L}_{\mathsf{sk}} := \emptyset} \\ & 2:\ (\mathsf{pp},\mathsf{msk}) \leftarrow \mathsf{Setup}(1^{\kappa}) \\ & 3:\ (\mathsf{id}^*,\mathsf{m}^*,\sigma^*) \leftarrow \mathcal{A}^{\{\mathcal{Q}_{\mathsf{sgn}},\mathcal{Q}_{\mathsf{key}}\}}(1^{\kappa},\mathsf{pp}) \\ & 4:\ \mathsf{if}\ \mathsf{id}^* \in \mathcal{Q}_{\mathsf{key}}\ \mathsf{or}\ (\mathsf{id}^*,\mathsf{m}^*) \in \mathcal{Q}_{\mathsf{sign}} \\ & \mathsf{then} \\ & 5:\ \ \mathsf{return}\ 0 \\ & 6:\ \mathsf{end}\ \mathsf{if} \\ & 7:\ \mathsf{return}\ \mathsf{Ver}(\mathsf{pp},\mathsf{id}^*,\mathsf{m}^*,\sigma^*) \end{split}
```

EUF-ID-CMA: More Details

Algorithms:

- Setup(κ) \rightarrow (pp, msk)
- $\bullet \; \; \mathsf{KeyGen}(\mathsf{pp},\mathsf{msk},\mathsf{id}) \to \mathsf{sk}_\mathsf{id}$
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- $\bullet \ \, \mathsf{Ver}(\mathsf{pp}, m, \sigma, \mathsf{id}) = \begin{cases} 1 & \mathsf{accept} \\ 0 & \mathsf{reject.} \end{cases}$

$\mathsf{Exp}^{\mathrm{EUF\text{-}ID\text{-}CMA}}_{\mathcal{A}}(\kappa)$:

- 1: $Q_{\text{key}} := \emptyset$, $Q_{\text{sign}} := \emptyset$, $\mathcal{L}_{\text{sk}} := \emptyset$
- 2: $(pp, msk) \leftarrow Setup(1^{\kappa})$ 3: $(id^*, m^*, \sigma^*) \leftarrow \mathcal{A}^{\{\mathcal{O}_{sign}, \mathcal{O}_{key}\}}(1^{\kappa}, pp)$
- 4: **if** $\mathsf{id}^* \in \mathcal{Q}_{\mathsf{key}}$ or $(\mathsf{id}^*, \mathsf{m}^*) \in \mathcal{Q}_{\mathsf{sign}}$ then
 - 5: return 0
- 6: end if
- 7: **return** $Ver(pp, id^*, m^*, \sigma^*)$

$\mathcal{O}_{\text{key}}(\text{id})$:

- 1: if id $\notin \mathcal{Q}_{key}$ then
- 2: $Q_{key} := Q_{key} \cup \{id\}$
- 3: end if
- 4: if $(id, sk_{id}) \in \mathcal{L}_{sk}$ then
- 5: **return** sk_{id}
- 6: end if
- 7: $sk_{id} \leftarrow KeyGen(pp, msk, id)$
- 8: $\mathcal{L}_{\mathsf{sk}} := \mathcal{L}_{\mathsf{sk}} \cup \{(\mathsf{id}, \mathsf{sk}_{\mathsf{id}})\}$
- 9: return skid

$\mathcal{O}_{\mathsf{sign}}(\mathsf{id}, \mathsf{m})$:

- 1: if $(id, m) \notin Q_{sign}$ then
- 2: $\mathcal{Q}_{\mathsf{sign}} := \mathcal{Q}_{\mathsf{sign}} \cup \{(\mathsf{id}, \mathrm{m})\}$
- 3: end if
 4: if (id, sk_{id}) ∉ L_{sk} then
- 5: sk_{id} ← KeyGen(pp, msk, id)
- 6: $\mathcal{L}_{sk} := \mathcal{L}_{sk} \cup \{(id, sk_{id})\}$
- 7: end if
- 8: $return Sign(pp, m, sk_{id})$

EUF-ID-CMA: More Details

```
Algorithms:
                                                                                  1: \mathcal{Q}_{kev} := \emptyset, \mathcal{Q}_{sign} := \emptyset, \mathcal{L}_{sk} := \emptyset
    • Setup(\kappa) \rightarrow (pp, msk)
                                                                                  2: (pp, msk) \leftarrow Setup(1^{\kappa})

    KeyGen(pp, msk, id) → sk<sub>id</sub>

                                                                                  3: (id^*, m^*, \sigma^*) \leftarrow \mathcal{A}^{\{\mathcal{O}_{sign}, \mathcal{O}_{key}\}}(1^{\kappa}, pp)
                                                                                  4: if id^* \in \mathcal{Q}_{\mathsf{kev}} or (id^*, m^*) \in \mathcal{Q}_{\mathsf{sign}}
    • Sign(pp, m, sk<sub>id</sub>) \rightarrow \sigma
                                                                                       then
    • Ver(pp, m, \sigma, id) = \begin{cases} 1 & accept \\ 0 & reject. \end{cases}
                                                                                             return 0
                                                                                  6: end if
                                                                                  7: return Ver(pp. id*, m*, \sigma*)
\mathcal{O}_{\text{kev}}(\text{id}):
                                                                                \mathcal{O}_{\mathsf{sign}}(\mathsf{id}, \mathsf{m}):
1: if id \notin Q_{kev} then
                                                                                  1: if (id, m) \notin \mathcal{Q}_{\text{sign}} then
 2: Q_{key} := Q_{key} \cup \{id\}
                                                                                  2: Q_{sign} := Q_{sign} \cup \{(id, m)\}
 3: end if
                                                                                  3: end if
 4: if (id, sk_{id}) \in \mathcal{L}_{sk} then
                                                                                  4: if (id, sk_{id}) \notin \mathcal{L}_{sk} then
             return skid
                                                                                  5: sk<sub>id</sub> ← KeyGen(pp, msk, id)
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 8: \mathcal{L}_{\mathsf{sk}} := \mathcal{L}_{\mathsf{sk}} \cup \{(\mathsf{id}, \mathsf{sk}_{\mathsf{id}})\}
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According to the definition of IBS, a user with identity id generates signatures
on (id, m) for different messages m using the same private key skid, and this
environment is correctly captured by the EUF-ID-CMA model [BNN04, LPLL20].

Non-Adaptive Model: EUF-naCMA

```
\mathsf{Exp}_{A}^{\mathsf{EUF}\text{-}\mathsf{naCMA}}(\kappa):
 1: (Q_{\text{key}}, Q_{\text{sign}}) \leftarrow \mathcal{A}(1^{\kappa})
  2: (pp, msk) \leftarrow Setup(1^{\kappa})
  3: for id \in \mathcal{Q}_{key} do
  4: sk<sub>id</sub> ← KeyGen(pp, msk, id)
  5: \mathcal{L}_{\mathsf{sk}} := \mathcal{L}_{\mathsf{sk}} \cup \{\mathsf{sk}_{\mathsf{id}}\}
  6: end for
  7: for (id, m) \in \mathcal{Q}_{\text{sign}} do
  8: \sigma \leftarrow \mathsf{Sign}(\mathsf{pp}, \mathsf{m}, \mathsf{sk}_{\mathsf{id}})
  9: \mathcal{L}_{sign} := \mathcal{L}_{sign} \cup \{\sigma\}
10: end for
11: (id^*, m^*, \sigma^*) \leftarrow \mathcal{A}(pp, \mathcal{L}_{sk}, \mathcal{L}_{sign})
12: if id^* \in \mathcal{Q}_{kev} or (id^*, m^*) \in \mathcal{Q}_{sign} then
13:
               return 0
14: end if
15: return Ver(pp, id, m, \sigma)
```

$$\mathsf{Adv}^{\mathrm{EUF\text{-}naCMA}}_{\mathcal{A}}(\kappa) := \mathsf{Pr}\left[\mathsf{Exp}^{\mathrm{EUF\text{-}naCMA}}_{\mathcal{A}}(\kappa) = 1\right]$$

• The scheme is EUF-naCMA secure, if for all ppt \mathcal{A} , $Adv_{\mathcal{A}}^{\mathrm{EUF-naCMA}}(\kappa)$ is negligible.

Generic Constructions of IBS: Adaptive Security

Several generic techniques have been proposed to construct IBS from different primitives:

- Bellare, Namprempre, and Neven (2004, 2009) proposed two generic techniques for IBS:
 - Using digital signatures at two levels: one for generating public parameters and the master secret key, and another for generating keys for individual identities.
 - Based on a standard identification scheme combined with a trapdoor sampleable relation (TSR), followed by the Fiat-Shamir transform.

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 - Based on a standard identification scheme combined with a trapdoor sampleable relation (TSR), followed by the Fiat-Shamir transform.
- However, these generic approaches lack tight security reductions.

Generic Constructions of IBS: Adaptive and Tight Security

- Note that tightly secure cryptographic schemes offer better concrete security assurance than their non-tight counterparts.
- Zhang et al. (2019) proposed a generic construction of IBS using two digital signatures: one secure in the single-user setting and the other in the multi-user setting.
- Later, Lee et al. (2020) showed that the same construction achieves tight security in the EUF-ID-CMA model.
- However, the construction is not efficient as each signature includes the underlying public key.

Generic Constructions of Pan and Wagner (2021)

This work claims to realize tightly EUF-ID-CMA secure IBS schemes from lattices using a two-stage approach:

- First, construct an IBS scheme from lattices achieving a tight reduction in a **non-adaptive** security model.
- Then, lift such scheme to tight adaptive security (EUF-ID-CMA) using two generic approaches:
 - One based on chameleon hashes in the standard model (SM).
 - The other based on hash functions in the random oracle model (ROM).

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 - The other based on hash functions in the random oracle model (ROM).

Note: The above result has recently been extended (SPMC-ACNS23) to the QROM.

Issues in Adaptive Model of PW21

```
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Issue in EUF-ID-CMA-PW

- For answering two (or more) signing queries on the same identity but for different messages, a fresh key is generated each time.
- When A makes a sign query followed by a key query on the same identity, the returned signing key is different from the one used to generate the signature.

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- Tor answering two (or more) signing queries on the same identity but for different messages, a fresh key is generated each time.
- When A makes a sign query followed by a key query on the same identity, the returned signing key is different from the one used to generate the signature.
- In either case, the security model deviates from the standard EUF-ID-CMA model and, therefore, does not accurately capture the real protocol environment.

Reduction Outline of PW21

- Both reductions are invalid in EUF-ID-CMA, though they remain valid in their proposed model, EUF-ID-CMA-PW.
- The issue is illustrated using their chameleon hash-based construction.

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- Let IBS' = (IBS'.Setup, IBS'.KeyGen, IBS'.Sign, IBS'.Ver) be a non-adaptively secure primitive identity-based signature scheme with identity space \mathcal{ID}' and message space \mathcal{M}' .
- Let CHF = (CHGen, CHash, CHColl) be a chameleon hash function.

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- Let CHF = (CHGen, CHash, CHColl) be a chameleon hash function.
- Let IBS = (IBS.Setup, IBS.KeyGen, IBS.Sign, IBS.Ver) denote the target IBS scheme constructed using chameleon hash functions and the primitive IBS scheme IBS'.

Reduction Outline of PW21 (Cont.)

```
IBS.Setup(\kappa):
                                                                       IBS.Sign(pp, m, skid):
 1: (hk, td) \leftarrow CHGen(\kappa)
                                                                         1: parse sk_{id} as sk_{id} = (sk_{id'}, r)
 2: (pp', msk') \leftarrow IBS'.Setup(\kappa)
                                                                         2: s \stackrel{\text{U}}{\longleftarrow} \text{SaltSp}
 3: pp := (pp', hk) and msk := msk'
                                                                         3: m' \leftarrow CHash(hk, m; s)
 4: return (pp, msk)
                                                                         4: \sigma' \leftarrow \mathsf{IBS'}.\mathsf{Sign}(\mathsf{pp'}, \mathsf{m'}, \mathsf{sk}_{\mathsf{id'}})
                                                                         5: \sigma := (\sigma', r, s)
IBS.KeyGen(pp, msk, id):
                                                                         6: return \sigma
 1: r \stackrel{\text{U}}{\longleftarrow} \text{SaltSp}
                                                                       IBS. Ver(pp, id, m, \sigma):
 2: id' \leftarrow CHash(hk, id; r)
                                                                         1: parse \sigma as \sigma = (\sigma', r, s)
 3: sk_{id'} \leftarrow IBS'.KeyGen(pp', msk', id')
                                                                         2: id' \leftarrow CHash(hk, id; r)
 4: sk_{id} := (sk_{id'}, r)
                                                                         3: m' \leftarrow CHash(hk, m; s)
 5: return skid
                                                                         4: return IBS'. Ver(pp', id', m', \sigma')
```

Reduction Outline of PW21 (Cont.)

```
IBS.Setup(\kappa):
                                                                        IBS.Sign(pp, m, sk_{id}):
                                                                         1: parse sk_{id} as sk_{id} = (sk_{id'}, r)
 1: (hk, td) \leftarrow CHGen(\kappa)
 2: (pp', msk') \leftarrow IBS'.Setup(\kappa)
                                                                         2: s \overset{\text{U}}{\longleftarrow} \mathsf{SaltSp}
 3: pp := (pp', hk) and msk := msk'
                                                                         3: m' \leftarrow CHash(hk, m; s)
 4: return (pp, msk)
                                                                         4: \sigma' \leftarrow \mathsf{IBS'}.\mathsf{Sign}(\mathsf{pp'}, \mathsf{m'}, \mathsf{sk}_{\mathsf{id'}})
                                                                         5: \sigma := (\sigma', r, s)
IBS.KeyGen(pp, msk, id):
                                                                         6: return σ
 1: r \stackrel{\text{U}}{\longleftarrow} \text{SaltSp}
                                                                       IBS. Ver(pp, id, m, \sigma):
 2: id' \leftarrow CHash(hk, id; r)
                                                                         1: parse \sigma as \sigma = (\sigma', r, s)
 3: sk_{id'} \leftarrow IBS'.KeyGen(pp', msk', id')
                                                                         2: id' \leftarrow CHash(hk, id; r)
 4: sk_{id} := (sk_{id'}, r)
                                                                         3: m' \leftarrow CHash(hk, m; s)
 5: return skid
                                                                         4: return IBS'. Ver(pp', id', m', σ')
```

- ① At the beginning, a simulator S declares Q'_{key} and Q'_{sign} in the EUF-naCMA game against IBS' and obtains the corresponding keys and signatures.
- ② Specifically, S prepares the *i*-th entry of Q'_{sign} as follows: $\text{id}'_i = \text{CHash}(\text{hk}, 0; r'_i)$ and $m'_i = \text{CHash}(\text{hk}, 0; s'_i)$, where r'_i and s'_i are random salts.
- 3 Let σ'_i denote the signature that S obtains for (id'_i, m'_i) from its challenger.

Reduction Outline of PW21 (Cont.)

```
IBS.Setup(\kappa):
                                                                       IBS.Sign(pp, m, skid):
 1: (hk, td) \leftarrow CHGen(\kappa)
                                                                         1: parse sk_{id} as sk_{id} = (sk_{id'}, r)
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                                                                         2: s \stackrel{\text{U}}{\longleftarrow} \text{SaltSp}
 3: pp := (pp', hk) and msk := msk'
                                                                         3: m' \leftarrow CHash(hk, m; s)
 4: return (pp, msk)
                                                                         4: \sigma' \leftarrow \mathsf{IBS'}.\mathsf{Sign}(\mathsf{pp'}, \mathsf{m'}, \mathsf{sk}_{\mathsf{id'}})
                                                                         5: \sigma := (\sigma', r, s)
IBS.KeyGen(pp, msk, id):
                                                                         6: return \sigma
 1: r \stackrel{\text{U}}{\longleftarrow} \text{SaltSp}
                                                                       IBS. Ver(pp, id, m, \sigma):
 2: id' \leftarrow CHash(hk, id; r)
                                                                         1: parse \sigma as \sigma = (\sigma', r, s)
 3: sk_{id'} \leftarrow IBS'.KeyGen(pp', msk', id')
 4: sk_{id} := (sk_{id'}, r)
                                                                         2: id' \leftarrow CHash(hk, id; r)
                                                                         3: m' \leftarrow CHash(hk, m; s)
 5: return skid
                                                                         4: return IBS'.Ver(pp', id', m', \sigma')
```

- **1** Later, when \mathcal{A} makes the *i*-th signature query on some message (id_i, m_i), S utilizes the trapdoor td to correctly map (id'_i, m'_i).
- **⑤** Specifically, using td, S finds r_i and s_i such that CHash(hk, id_i; r_i) = id'_i and CHash(hk, m_i; s_i) = m'_i, and returns $\sigma_i = (\sigma'_i, r_i, s_i)$ to \mathcal{A} .
- \odot A similar approach is applicable in preparing $\mathcal{Q}'_{\text{kev}}$ and answering key queries.

- Case I: A makes the *i*-th and *j*-th signature queries on the same identity as (id, m_i) and (id, m_i):
 - As per the protocol, the same secret key sk_{id} has to be used to generate the two signatures.
 - Hence, the same randomizer r must be included as part of the two returned signatures.
 - However, the randomizers are different as the two queries are respectively mapped to the *i*-th and *j*-th elements of Q'_{sign} :

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 - Hence, the same randomizer r must be included as part of the two returned signatures.
 - However, the randomizers are different as the two queries are respectively mapped to the *i*-th and *j*-th elements of Q'_{sign} :
 - S first has to compute $r_1 = CHColl(hk, td, 0, r_i, id)$ and $r_2 = CHColl(hk, td, 0, r_j, id)$.
 - Clearly, r₁ ≠ r₂ with overwhelming probability due to the property of chameleon hash function.

- Case II: A first makes a signature query on some identity id, followed by a key query on id:
 - According to the protocol, the secret key returned for the key query on id must be the same as the one used to respond to the preceding signature query.
 - This implies that the salt component *r* in both responses must be identical.
 - However, in the reduction presented in [PW21], the two queries produce different randomizers *r*.
- Thus, it violates the actual protocol environment as well as the standard EUF-ID-CMA model.

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Remark: A similar argument is applicable to the ROM-based reduction of [PW21].

Tight Security in a Restrictive Yet Realistic Model

- We show that a tight reduction is possible in a restricted version of the standard EUF-ID-CMA model.
- **WModel I:** This is the same as the EUF-ID-CMA model, except that $Q_{\text{kev}} \cap Q_{\text{id}} = \emptyset$.
- We show that both generic constructions of [PW21] achieve tight security in WModel I.

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- We show that a tight reduction is possible in a restricted version of the standard EUF-ID-CMA model.
- WModel I: This is the same as the EUF-ID-CMA model, except that $\mathcal{Q}_{\text{key}} \cap \mathcal{Q}_{\text{id}} = \emptyset$.
- We show that both generic constructions of [PW21] achieve tight security in WModel I.
- Note that the original reductions from [PW21] cannot go through this model, even though it appears to be a weak model.
 - For example, if A makes all signature queries with the same identity, the salt parts r will differ for all the replied signatures
 which is a violation w.r.t WModel I.
 - On the other hand, our reductions consider q_s^2 signature calls in EUM-naCMA against q_s signature calls in **WModel I** to correctly handle the above scenario.

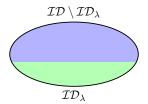
Lifting Reductions from WModel-I to EUF-ID-CMA

WModel I: $Q_{\text{key}} \cap Q_{\text{id}} = \emptyset$ C - EUF-naCMA Challenger A – EUF-ID-CMA Attacker S – Simulator

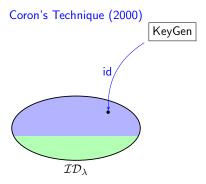
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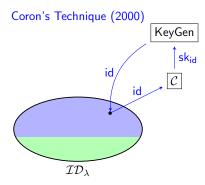
Coron's Technique (2000)



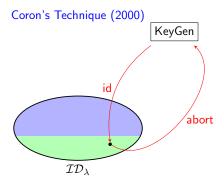
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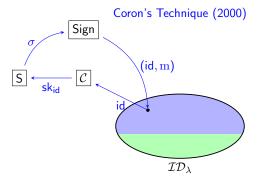


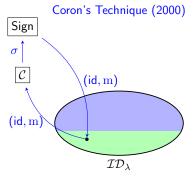
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WModel I: $Q_{\text{kev}} \cap Q_{\text{id}} = \emptyset$ A – EUF-ID-CMA Attacker C − EUF-naCMA Challenger 5 - Simulator Coron's Technique (2000) Sign (id, m)

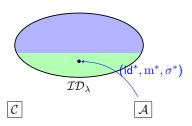
 \mathcal{ID}_{λ}



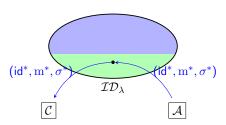


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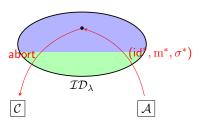


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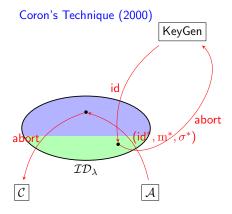


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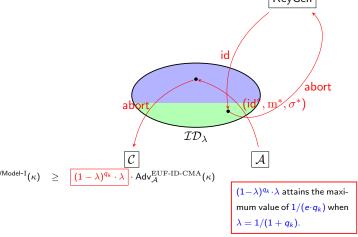
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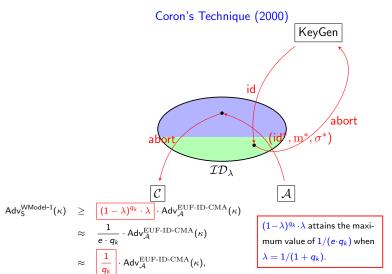
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Coron's Technique (2000) KeyGen id abort (id*, m* \mathcal{ID}_{λ} $(1-\lambda)^{q_k} \cdot \lambda \cdot \mathsf{Adv}^{\mathrm{EUF\text{-}ID\text{-}CMA}}_{\mathcal{A}}(\kappa)$



WModel I: $Q_{\text{key}} \cap Q_{\text{id}} = \emptyset$ C - EUF-naCMA Challenger A – EUF-ID-CMA AttackerS – Simulator



- Consider the following two scenarios:
 - $oldsymbol{1}$ \mathcal{A} first makes a sign query on some (id, m) followed by a key query on the same identity id.
 - ${f 2}$ ${\cal A}$ is likely to make sign queries on certain identities but not a follow-up key query.

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- This entails a degradation in the reduction which is proportional to either q_k or q_s .

Conclusion

- Pan and Wagner proposed a generic conversion from non-adaptive to adaptively secure IBS with a tightness claim.
- We identified certain gaps in their approach and proposed new reductions to address these gaps.
- We argued why the technique of [PW21] is unlikely to yield a tight reduction in the EUF-ID-CMA model.
- Additionally, we proposed a functional extension of the Pan-Wagner technique, enabling the registration of multiple devices under the same identity.

Thank you for your kind attention!

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Contact Email: tapas.pandit@plaksha.edu.in